#### Exam 1 Review

## Exam 1 details:

- 5-6 pages of questions
- ONLY the Ti-30x IIS Calculator model is allowed (and required)
- Allowed one hand-written 8.5 by 11 in. page (double-sided)
- You must show your work on all problems.
- Covers 10.1, 2.1-2.3, 2.5-2.8 3.1-3.3. You should know all the facts and concepts covered in the homework for those sections.
- You have 80 minutes to complete the exam.

## Studying Advice:

- Spend 15-30 minutes reviewing all homework.
- Spend 15-30 minutes flipping through 8+ old exams.
- Spend several hours working through several old exams in detail.
- Practice managing your time, never spend more than 10 minutes on a page!

#### Exam 1 Basic Facts

- 1. Precalculus: Know all the standard functions, know trig and trig values, know your algebra skills, know circular motion and basic parametric facts.
- 2. Limit Foundations: Know limit notation, be able to get limits from the picture of a graph, know definitions.
- 3. Finite Limits: Know techniques ?/0, 0/0, factoring, expanding, conjugate, fractions.
- 4. Limits at Infinity: Know techniques for  $\infty/\infty$ , identify known limits, divide top/bottom
- 5. Continuity and Differentiability: Know what these terms mean!
- 6. Derivative Foundations: What is  $\frac{f(x+h)-f(x)}{h}$ , be able to compute this for a given function.
- 7. The derivative graph: Know the connections between the graphs of f(x) and f'(x).
- 8. Derivative Rules: Know the sum and coefficient rules, the power rule, the exponential rule, all trig, the product rule and the quotient rule.
- 9. Applications: Know units of derivative, understand what it represents as a rate, be able to do tangent line questions.

### Basic Precalculus:

- 1. Power/exponent rules.
- 2. Solving equations (using inverses and the quadratic formula)
- 3. Understanding what  $x = \cos(t)$  and  $y = \sin(t)$  gives.
- 4. Knowing standard trig rules and values (unit circle)
- 5. Factoring/Expanding/Conjugate
- 6. Basics of plotting parametric points
- 7. Functional Notation!

#### Limits:

First, see my previous postings on the course website reviewing limits.

- 1. 'Plug in'
- 2. If it approaches ?/0 and the numerator is not zero, then examine the sign of the expression from both sides  $(-\infty, +\infty, \text{ or DNE})$ .
- 3. If it appoaches 0/0, then use factoring, expanding, conjugates, and simplifying fractions to eliminate the zero in the denominator if possible.
- 4. If it approaches  $\infty/\infty$ , then divide top and bottom by  $1/x^a$  or  $1/e^{rx}$  and try to rewrite the expression in terms of known functions.
- 5. Know the standard precalculus functions, it helps!
- 6. Know that  $\lim_{x\to 0} \frac{\sin(x)}{x} = 1$

## **Derivative Foundations and Basic Facts:**

- 1. What is  $\frac{f(x+h)-f(x)}{h}$ ? What does it represent graphically? What does it represent in an applied problem with units?
- 2. What is  $\lim_{h\to 0} \frac{f(x+h)-f(x)}{h}$ ? Same questions as above.
- 3. What are the connections between the graphs of f(x) and f'(x)?

# Continuity/Differentiability:

- 1. Know what it means to be continuous at a point. How do we check it?
- 2. Know what it means to be differentiable at a point. How do we check it?

### Derivative Rules

- 1. What are the sum and coefficient rules?
- 2. What are the product and quotient rules?
- 3. What is the derivative of  $x^n$ ?
- 4. What is the derivative of  $a^x$ ?
- 5. What is the derivative of the 6 trig functions?

# **Applied Questions:**

- 1. Find the equation for a tangent line given a point on the curve.
- 2. Find the equation for a tangent line given a point on the line, but off the curve.
- 3. Set up a problem involving trig or a circle or something from precalculus and do a limit or a derivative.